

2-7-2024

## Reliability of offshore plate anchor design in sand for uplift limit state

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### Recommended Citation

LI, Yu-ting; CHEN, Xiao-bin; and HE, Peng-peng (2024) "Reliability of offshore plate anchor design in sand for uplift limit state," *Rock and Soil Mechanics*: Vol. 44: Iss. 12, Article 3.

DOI: 10.16285/j.rsm.2023.00320

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### Abstract

The offshore wind industry needs to move towards floating offshore wind turbines (FOWTs) that are secured to the seabed with anchoring systems in order to harness the more substantial amounts of offshore wind resources available in deep waters. The design of the anchoring system for FOWTs is crucial to ensure stability and safety in challenging offshore conditions. As a simplified reliability-based design approach, the partial safety factor method remains important in current offshore foundation design practice, but its effectiveness in achieving the required target safety level still needs to be examined. To achieve this end, a reliability analysis is performed for the uplift limit state design of strip plate anchors embedded in sand subjected to vertical loads, and a wide range of load cases are considered in the analysis. The failure probabilities of strip plate anchors designed with the partial safety factor method are estimated and then compared to the target safety levels. The results show that the estimated reliability index decreases rapidly with the increasing of permanent to variable action ratio and gradually converges to a relatively steady state. In addition, the current partial safety factor method has been shown to be conservative for offshore plate anchor design over a wide range of permanent to variable action ratios. The results provide probabilistic insights into the effectiveness of the partial safety factor method and may aid in the further development of reliability analysis for offshore anchors.

### Keywords

reliability analysis, partial safety factor method, uplift limit state, offshore plate anchors, drainage conditions

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**Abstract:** The offshore wind industry needs to move towards floating offshore wind turbines (FOWTs) that are secured to the seabed with anchoring systems in order to harness the more substantial amounts of offshore wind resources available in deep waters. The design of the anchoring system for FOWTs is crucial to ensure stability and safety in challenging offshore conditions. As a simplified reliability-based design approach, the partial safety factor method remains important in current offshore foundation design practice, but its effectiveness in achieving the required target safety level still needs to be examined. To achieve this end, a reliability analysis is performed for the uplift limit state design of strip plate anchors embedded in sand subjected to vertical loads, and a wide range of load cases are considered in the analysis. The failure probabilities of strip plate anchors designed with the partial safety factor method are estimated and then compared to the target safety levels. The results show that the estimated reliability index decreases rapidly with the increasing of permanent to variable action ratio and gradually converges to a relatively steady state. In addition, the current partial safety factor method has been shown to be conservative for offshore plate anchor design over a wide range of permanent to variable action ratios. The results provide probabilistic insights into the effectiveness of the partial safety factor method and may aid in the further development of reliability analysis for offshore anchors.

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## 1 Introduction

Offshore wind turbines have experienced significant growth in the past two decades to address the climate change concerns and to achieve the net zero carbon emissions target<sup>[1]</sup>. To withstand harsh environmental conditions such as sea wave, wind, and current, fixed-bottom wind turbines are mostly adopted for water depths up to 60 m. However, they become less feasible for deeper waters due to the significant cost increase and difficulty of installation<sup>[2]</sup>. Therefore, the offshore wind industry needs to move towards floating offshore wind turbines (FOWTs) that are secured to the seabed with anchoring systems in order to harness the more substantial amounts of offshore wind resources available in deeper waters. For FOWTs, the design of the anchoring system is crucial to ensure stability and safety in challenging offshore conditions<sup>[3]</sup>.

Reliable plate anchor design involves considering various sources of uncertainties, such as uncertainties related to soil variability, site investigation, anchor installation, prediction models, and various loads. The conventional design method of using a global factor of safety may not be sufficient to account for these uncertainties and is less rational compared to the reliability-based approach that

makes use of probability theories<sup>[4]</sup>. As a more sophisticated design method that explicitly addresses various uncertainties<sup>[5]</sup>, the reliability-based design approach has the potential to produce more cost-effective and consistent design across different site conditions<sup>[6–7]</sup>. Some reliability analyses have been performed for offshore foundations recently<sup>[8–10]</sup>. The partial safety factor approach can be considered as a simplified reliability-based design approach, which is a trade-off between the conventional global factor of safety method and the reliability-based design approach. It allows separate consideration of uncertainties in soil and loads, and retains the simplicity of performing algebraic design checks. As a result, the partial safety factor method remains important in current offshore foundation design practice<sup>[11]</sup>. However, it is crucial to ensure the effectiveness of this simplified method in achieving the required target safety level.

This paper performs a reliability analysis of offshore plate anchors to investigate whether the current design developed using the partial safety factor method meets the required target safety levels. The study concentrates on the uplift limit state design of strip plate anchors embedded in sand subjected to vertical loads. A wide range of load cases are considered in the analysis. The results provide probabilistic insights into the effectiveness

Received: 3 July 2023

Accepted: 31 October 2023

This work was supported by the Science and Technology Research and Development Plan of China Railway Co., Ltd. (2022-Major Project-07).

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of the partial safety factor method and may aid in the further development of reliability analysis for offshore anchors.

## 2 Uplift resistance of strip plate anchors

White et al.<sup>[12]</sup> obtained a limit equilibrium solution for the uplift resistance of strip plate anchors by assuming that the shear planes of the failed block are inclined at the dilation angle  $\psi$ . The peak uplift resistance per unit length  $R_u$ , is computed as

$$\frac{R_u}{\gamma'HB} = N_\gamma = 1 + F_u \frac{H}{B} \quad (1)$$

where  $N_\gamma$  is a dimensionless uplift factor;  $\gamma'$  is the soil effective unit weight;  $H$  is the anchor embedment depth;  $B$  is the strip anchor width; and  $F_u$  is an uplift factor expressed as

$$F_u = \tan \psi_p + (\tan \varphi_p - \tan \psi_p) \left( \frac{1+K_0}{2} - \frac{1-K_0}{2} \cos(2\psi_p) \right) \quad (2)$$

where  $\varphi_p$  is the peak friction angle of sand;  $\psi_p$  is the peak dilation angle of sand; and  $K_0$  is the lateral earth pressure coefficient at rest, which is calculated as  $K_0 = 1 - \sin \varphi_{cs}$  with  $\varphi_{cs}$  being the critical state friction angle of sand.

White et al.<sup>[12]</sup> further applied the stress–dilatancy relationships (Eq. (3)) proposed by Bolton<sup>[13]</sup> to transform the peak uplift resistance as a function of the soil relative density  $I_D$  and  $\varphi_{cs}$ .

$$\left. \begin{aligned} \varphi_p - \varphi_{cs} &= k\psi_p \\ \varphi_p - \varphi_{cs} &= mI_R \end{aligned} \right\} \quad (3)$$

where  $I_R$  is a relative dilatancy index as a function of the soil relative density  $I_D$ , grain-crushing strength  $\sigma'_c$ , and the mean effective strength  $p'$ ,  $I_R = I_D \ln(\sigma'_c/p') - 1$ . The parameters  $k$  and  $m$  are taken as 0.8 and 5, respectively, under plane strain conditions in this analysis.

Manipulating Eqs. (1)–(3) to eliminate  $\psi_p$  re-writes the peak uplift resistance as a function of  $I_D$  or  $\varphi_p$ . Since the range of the variability of  $\varphi_p$  has been extensively studied with greater confidence than that of  $I_D$ , the peak uplift resistance is expressed as a function of  $\varphi_p$ . The uplift factor is re-written as

$$F_u = \tan \frac{\varphi_p - \varphi_{cs}}{k} + \left( \tan \varphi_p - \tan \frac{\varphi_p - \varphi_{cs}}{k} \right) \left[ \frac{1+K_0}{2} - \frac{1-K_0}{2} \cos \frac{2(\varphi_p - \varphi_{cs})}{k} \right] \quad (4)$$

Recall that  $K_0$  is taken as a function of  $\varphi_{cs}$  to be  $K_0 = 1 - \sin \varphi_{cs}$ . The critical state friction angle  $\varphi_{cs}$  is a fundamental soil property depending primarily on particle mineralogy and shape. It has been determined experimentally to be

around  $33^\circ$  for quartz and  $40^\circ$  for feldspar within a margin of  $1^\circ$ <sup>[13]</sup>. Therefore,  $\varphi_{cs}$  can be regarded as a deterministic parameter in the analysis, and the peak friction angle,  $\varphi_p$ , is discussed in the following section.

## 3 Characteristic values of soil parameters and load

The peak uplift resistance of a strip plate anchor in sand calculated with Eqs. (1) and (4) is primarily affected by two parameters, i.e. the soil peak friction angle,  $\varphi_p$ , and the soil effective unit weight,  $\gamma'$ , which are represented by two random variables, characterised by their means and standard deviations. Since  $\gamma'$  is constrained to non-negative values, it is assumed to be lognormally distributed with a mean  $\mu_{\gamma'}$  and a standard deviation  $\sigma_{\gamma'}$ <sup>[14]</sup>. Reference<sup>[15]</sup> recommends a “cautious estimate of the mean” for the characteristic values of geotechnical parameters, and further states that the characteristic values of geotechnical parameters should be selected to ensure at least a 95% confidence in the geotechnical system for a limit state considered in the design. This recommendation is fairly vague for design. When a low value of the material property is unfavourable, Reference<sup>[16]</sup> suggests the 5% fractile value for its characteristic value. Following the suggestion, the characteristic value of effective unit weight,  $\hat{\gamma}'$ , of the soil used for design is represented by the 5% fractile of its lognormal distribution:

$$\hat{\gamma}' = \exp[\mu_{\ln \gamma'}(1 - 1.645v_{\ln \gamma'})] \quad (5)$$

where  $\mu_{\ln \gamma'}$  and  $v_{\ln \gamma'} = \sigma_{\ln \gamma'} / \mu_{\ln \gamma'}$  are the mean and coefficient of variation of its normally distributed counterpart,  $\ln \gamma'$ , with  $\sigma_{\ln \gamma'}$  being the standard deviation. It should be noted that hat parameters are adopted for anchor design in this analysis. The lognormally distributed  $\gamma'$  can be transformed to its normally distributed counterpart, having parameters:

$$\left. \begin{aligned} \sigma_{\ln \gamma'}^2 &= \ln(1 + v_{\gamma'}^2) \\ \mu_{\ln \gamma'} &= \ln \mu_{\gamma'} - \frac{1}{2} \sigma_{\ln \gamma'}^2 \end{aligned} \right\} \quad (6)$$

where  $v_{\gamma'} = \sigma_{\gamma'} / \mu_{\gamma'}$  is the coefficient of variation of  $\gamma'$ .

Following Fenton et al.<sup>[17]</sup> and He et al.<sup>[18]</sup>, the peak friction angle  $\varphi_p$  is assumed to follow a bounded tanh distribution. The tanh distribution has a simple relationship with the normal distribution expressed as<sup>[19]</sup>

$$\varphi_p = \varphi_{p,\min} + \frac{1}{2}(\varphi_{p,\max} - \varphi_{p,\min}) \left[ 1 + \tanh \left( \frac{sG_\varphi}{2\pi} \right) \right] \quad (7)$$

where  $G_\varphi$  is the standard normal;  $\varphi_{p,\min}$  and  $\varphi_{p,\max}$  are the minimum and maximum peak friction angles, respectively;

and  $s$  is a scale factor governing the variability of  $\varphi_p$  between the two bounds<sup>[19]</sup>. The distribution is symmetric and has a mean of  $\mu_{\varphi_p} = (\varphi_{p,max} - \varphi_{p,min}) / 2$ . In this analysis,  $\varphi_p$  is assumed to be bounded between  $30^\circ$  and  $50^\circ$ <sup>[20]</sup> with a mean of  $\mu_{\varphi_p} = 40^\circ$ . The scale factor is assumed to be  $s = 2.5$ , resulting in a bounded bell shaped distribution with the standard deviation of  $\sigma_{\varphi_p} \approx 3.4^\circ$ , and the coefficient of variation of  $v_{\varphi_p} \approx 3.4^\circ / 40^\circ = 0.09$ , which lies within the variability ranges suggested by Lee et al.<sup>[21]</sup> and Phoon and Kulhawy<sup>[22]</sup>.

Similar to  $\gamma'$ , the characteristic value of peak friction angle,  $\hat{\varphi}_p$ , is taken as the 5% fractile of the bounded tanh distribution. This can be obtained by numerically solving  $F(\varphi_p) = 0.05$  where  $F(\varphi_p)$  is the cumulative distribution function of  $\varphi_p$  which can be derived from its probability density function based on Eq. (7). Generally,  $\varphi_p$  and  $\gamma'$  have a reasonably positive correlation, which reduces the estimated failure probabilities<sup>[23]</sup>. In this paper,  $\varphi_p$  and  $\gamma'$  are conservatively assumed to be independent.

DNV<sup>[11]</sup> specifies that the design of offshore plate anchors need to consider two types of loads, i.e. the mean line tension ( $F_T$ ) due to pretension and the effect of mean environmental loads, and the dynamic increase in the line tension ( $F_D$ ) due to oscillatory low-frequency and wave-frequency effects, as shown in Fig. 1.  $F_T$  and  $F_D$  are represented by two independent random variables, following lognormal distributions with means of  $\mu_{F_T}$  and  $\mu_{F_D}$ , and standard deviations of  $\sigma_{F_T}$  and  $\sigma_{F_D}$ , respectively.

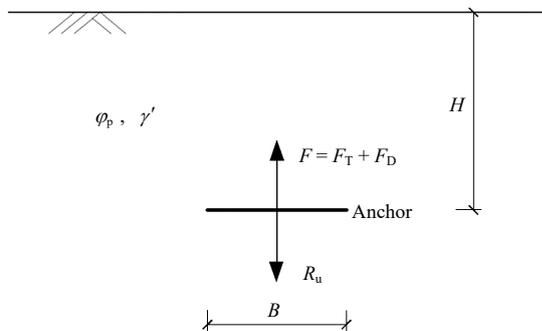


Fig. 1 Schematic diagram of strip plate anchor in sand under vertical uplift loads

As stated by Reference<sup>[16]</sup>, pre-stressing should be classified as a permanent action with the characteristic value equal to the 95% fractile of its statistical distribution. Therefore,  $F_T$  is taken as a permanent action, and its characteristic value  $\hat{F}_T$  used for design can be calculated by

$$\hat{F}_T = \exp[\mu_{\ln F_T} (1 + 1.645v_{\ln F_T})] \tag{8}$$

where  $\mu_{\ln F_T}$  and  $v_{\ln F_T}$  are the mean and coefficient of variation of the normally distributed  $\ln F_T$ , and can be calculated using the same form of Eq. (6) with respect

to  $F_T$ .

The characteristic value of dynamic line tension increment  $\hat{F}_D$  is assumed to be evaluated using the same method as  $\hat{F}_T$ , i.e.

$$\hat{F}_D = \exp[\mu_{\ln F_D} (1 + 1.645v_{\ln F_D})] \tag{9}$$

where  $\mu_{\ln F_D}$  and  $v_{\ln F_D}$  are the mean and coefficient of variation of the normally distributed  $\ln F_D$ , and can be calculated using the same form of Eq. (6) with respect to  $F_D$ .

### 4 Design of plate anchors

The general uplift limit state design criterion within the partial safety factor framework is expressed as

$$\hat{R}_u \left( \tan^{-1} \left( \frac{\tan \hat{\varphi}_p}{\gamma_\varphi} \right), \frac{\hat{\gamma}'}{\gamma_\gamma} \right) \geq \sum \gamma_{F_i} \hat{F}_i \tag{10}$$

where  $\hat{R}_u$  is the characteristic value of anchor uplift resistance as a function of  $\hat{\varphi}_p$  and  $\hat{\gamma}'$ ;  $\gamma_\varphi$  and  $\gamma_\gamma$  are the partial safety factors on  $\tan \hat{\varphi}_p$  and  $\hat{\gamma}'$ , respectively;  $\hat{F}_i$  is the  $i$ th characteristic load; and  $\gamma_{F_i}$  is the load partial factor corresponding to  $\hat{F}_i$ . It should be noted that  $\gamma_\varphi$  is applied to  $\tan \hat{\varphi}_p$  rather than  $\hat{\varphi}_p$  as stated by Reference<sup>[15]</sup>, thereby resulting in an equivalent characteristic value of peak friction angle equal to  $\tan^{-1}(\tan \hat{\varphi}_p / \gamma_\varphi)$ .

Since only  $F_T$  and  $F_D$  are considered for offshore anchor design, Eq. (10) is written more specifically as

$$\hat{R}_u \left( \tan^{-1} \left( \frac{\tan \hat{\varphi}_p}{\gamma_\varphi} \right), \frac{\hat{\gamma}'}{\gamma_\gamma} \right) \geq \gamma_T \hat{F}_T + \gamma_D \hat{F}_D \tag{11}$$

where  $\gamma_T$  and  $\gamma_D$  are the load partial factors corresponding to  $\hat{F}_T$  and  $\hat{F}_D$ , respectively.

As discussed previously,  $\hat{R}_u$  can be estimated using Eqs. (1) and (4) with  $\varphi_p$ ,  $\gamma'$ , and  $H$  replaced by  $\tan^{-1}(\tan \hat{\varphi}_p / \gamma_\varphi)$ ,  $\hat{\gamma}' / \gamma_\gamma$ , and  $\hat{H}$ , respectively.  $\hat{H}$  is the depth of the designed strip anchor. Note again that the hat parameters are used for the design process in this analysis.

The aim of the plate anchor design is to estimate the anchor embedment depth  $\hat{H}$ , that satisfies the design criterion in Eq. (11). Substituting Eqs. (1) and (4) into Eq. (11) at the equality yields the following equation:

$$\left( 1 + \hat{F}_u \frac{\hat{H}}{B} \right) \left( \frac{\hat{\gamma}'}{\gamma_\gamma} \hat{H} B \right) = \gamma_T \hat{F}_T + \gamma_D \hat{F}_D \tag{12}$$

In Eq. (12),  $\hat{F}_u$  is a function of  $\tan^{-1}(\tan \hat{\varphi}_p / \gamma_\varphi)$  (see Eq. (4)), and the strip anchor width  $B$  is assumed to be a deterministic value. Once the characteristic values of soil properties and loads are obtained from Section 3, the required anchor embedment depth  $\hat{H}$  is then estimated by numerically solving Eq. (12) for  $\hat{H}$  (see Fig. 2).

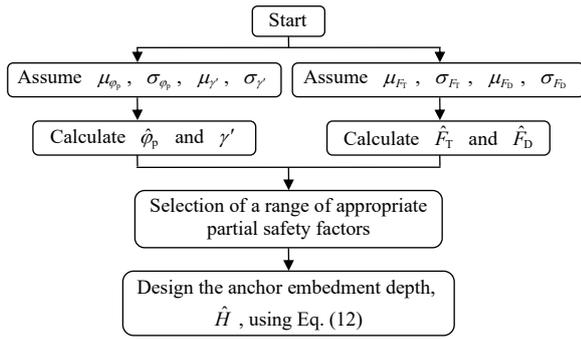


Fig. 2 Flowchart for plate anchor design

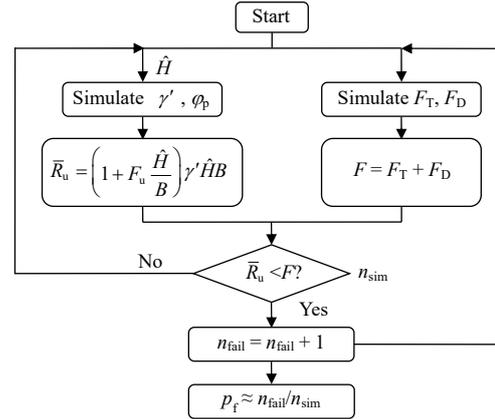


Fig. 3 Monte Carlo procedures

### 5 Estimate of failure probability

The failure probability of the designed anchor,  $p_f$ , is defined as the probability that the actual total load exceeds the actual anchor resistance of the designed anchor:

$$p_f = P[\bar{R}_u < F] \leq p_m \tag{13}$$

where  $\bar{R}_u$  is the actual (random) anchor uplift resistance estimated with the designed anchor embedment depth,  $\hat{H}$ ;  $F$  is the actual total vertical load,  $F = F_T + F_D$ , with  $F_T$  and  $F_D$  being the actual mean line tension and dynamic increment of the actual line tension, respectively; and  $p_m$  is the target maximum acceptable failure probability. Note that bar parameters are used for the actual values to differentiate from the design values in this analysis.

The actual uplift resistance  $\bar{R}_u$ , is estimated by Eq. (1), indicating that only the soil uncertainty is accounted for to calculate the failure probability without considering the uncertainty associated with the geotechnical prediction model. Using the same form of Eq. (1),  $\bar{R}_u$  is expressed as

$$\bar{R}_u = \left(1 + F_u \frac{\hat{H}}{B}\right) \gamma' \hat{H} B \tag{14}$$

where  $F_u$  is calculated using Eq. (4). It is worth noting that  $\bar{R}_u$  in Eq. (14) is evaluated based on the random variables,  $\phi_p$  and  $\gamma'$ , compared to the (deterministic) characteristic values,  $\hat{\phi}_p$  and  $\hat{\gamma}'$ , used for  $\hat{R}_u$ .

Once the designed anchor embedment depth,  $\hat{H}$ , is evaluated using Eq. (12), the failure probability,  $p_f$ , can be estimated with Monte Carlo simulations (see Fig. 3) following the steps below:

- (1) Simulate the random variables of the soil properties ( $\phi_p$  and  $\gamma'$ ), with the specified means and standard deviations, and evaluate the actual uplift resistance,  $\bar{R}_u$ , of the designed anchor using Eq. (14);
- (2) Simulate the actual  $F_T$  and  $F_D$ , and calculate the actual total vertical load,  $F = F_T + F_D$ ;
- (3) Determine whether the designed anchor fails ( $\bar{R}_u < F$ ); if so, update the number of failures, i.e.  $n_{fail} = n_{fail} + 1$ .

The above steps will be repeated  $n_{sim}$  times, and the failure probability of the designed plate anchor is then approximated to be  $p_f \approx n_{fail}/n_{sim}$ . The corresponding reliability index,  $\beta$ , is computed as

$$\beta = \Phi^{-1}(1 - p_f) \tag{15}$$

where  $\Phi$  is the cumulative distribution function of the standard normal.

### 6 Results and discussion

#### 6.1 Case study

As discussed in Section 1, the soil peak friction angle  $\phi_p$ , follows a bounded tanh distribution, ranging from  $30^\circ$  to  $50^\circ$  with a mean of  $\mu_{\phi_p} = 40^\circ$  and a coefficient of variation of  $v_{\phi_p} = 0.09$ . The effective unit weight,  $\gamma'$ , is assumed to have a mean of  $\mu_{\gamma'} = 8 \text{ kN/m}^3$  and a coefficient of variation of  $v_{\gamma'} = 0.1$ , which is aligned with the ranges summarised by Lee et al.<sup>[21]</sup> and Lumb<sup>[24]</sup>. The anchor width is assumed to be deterministic and is taken as  $B = 6 \text{ m}$ . In addition, Eqs. (5) and (6) give the characteristic value of effective unit weight of  $\hat{\gamma}' = 6.76 \text{ kN/m}^3$ . The characteristic value of peak friction angle is numerically obtained from the 5% fractile of the bounded tanh distribution shown in Eq. (7), which is  $\hat{\phi}_p = 34.25^\circ$ . As discussed previously, the critical state friction angle,  $\phi_{cs}$ , is assumed to be deterministic, which is taken as the lower bound of  $\phi_p$ , i.e.  $\phi_{cs} = 30^\circ$ .

The mean line tension  $F_T$  is assumed to have a mean of  $\mu_{F_T} = 500 \text{ kN/m}$ . The mean of the dynamic increment of line tension  $F_D$  is calculated as a certain portion of  $\mu_{F_T}$ , i.e.  $\mu_{F_D} = R_{D/T} \mu_{F_T}$  where  $R_{D/T}$  is the ratio of  $\mu_{F_D}$  to  $\mu_{F_T}$ . In this study, a wide range of  $R_{D/T}$  values from 0.2 to 3.0 is considered for a parametric study. Following the coefficient of variation ranges of different load effects for onshore and offshore foundations reported by Meyerhof<sup>[25]</sup>, the range of the coefficient of variation is 0.05–0.15 for permanent actions and 0.3–0.5 for environment loads.

In addition, higher values are expected for offshore loading conditions that are generally associated with a relatively higher level of uncertainty<sup>[26]</sup>. Recall that  $F_T$  is considered as a permanent action as suggested by Reference<sup>[16]</sup>, and  $F_D$  is expected to be more variable and is thus regarded as a variable action. The coefficients of variation of  $F_T$  and  $F_D$  are taken as  $v_{F_T} = 0.15$  and  $v_{F_D} = 0.5$ , respectively, which are conservatively at the higher ends of the above recommended ranges.

DNV<sup>[11]</sup> specifies two sets of partial safety factors in relation to two consequence classes for the uplift limit state design of plate anchors, as presented in Table 1 along with the corresponding target annual probabilities of failure,  $p_m$ . The partial safety factors for the effective unit weight and peak friction angle of the soil shown in Table 1 are provided by Reference<sup>[15]</sup> as DNV<sup>[11]</sup> does not consider drained soil conditions and soil unit weight.

It is worth noting that for uplift limit state design, only the load partial safety factors are different between the two consequence classes and the soil partial safety factors remain the same.

**Table 1 Partial safety factors and target failure probabilities for uplift limit state design of plate anchor**

Consequence class	$\gamma_\phi$	$\gamma_\gamma$	$\gamma_T$	$\gamma_D$	$p_m$
1	1.25	1.0	1.1	1.5	$10^{-4}$
2	1.25	1.0	1.4	2.1	$10^{-5}$

A total number of  $n_{sim} = 1 \times 10^8$  realisations is employed, which is able to reasonably accurately estimate failure probabilities down to around  $10/n_{sim} = 1 \times 10^{-7}$  with a standard deviation of the estimate appropriately equal to  $\sqrt{p_f / n_{sim}} = \sqrt{10^{-7} / 10^8} = 3.16 \times 10^{-8}$ . The above-mentioned input parameters are summarised in Table 2.

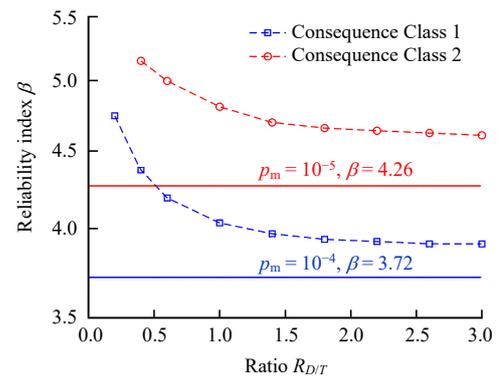
**Table 2 Input parameters for estimation of plate anchor failure probability**

$\mu_{\phi_p} / (^\circ)$	$\sigma_{\phi_p} / (^\circ)$	$\phi_{p,min} / (^\circ)$	$\phi_{p,max} / (^\circ)$	$s$	$\phi_{cs} / (^\circ)$	$\mu_\gamma / (\text{kN} \cdot \text{m}^{-3})$	$\sigma_\gamma / (\text{kN} \cdot \text{m}^{-3})$	$\mu_{F_T} / (\text{kN} \cdot \text{m}^{-1})$	$v_{F_T}$	$v_{F_D}$	$R_{D/T}$	$n_{sim}$
40	3.4	30	50	2.5	30	8	0.8	500	0.15	0.50	0.2–3.0	100 000 000

### 6.2 Results

Figure 4 shows the estimated reliability index of the strip plate anchor designed for uplift limit state using the partial safety factor method as a function of the ratio  $R_{D/T}$  for the two consequence classes. It can be seen that as the ratio  $R_{D/T}$  increases, the estimated reliability index presents a rapid decrease before gradually converging to a relatively steady state. More specifically, the reliability reaches  $\beta = 3.9$  for Consequence Class 1 and  $\beta = 4.6$  for Consequence Class 2. The primary reason is that increasing  $R_{D/T}$  makes the more variable  $F_D$  more dominant in the estimate of  $\beta$ , thereby reducing the estimate reliability index (increasing the estimate failure probability).

The target failure probabilities ( $p_m = 10^{-4} \rightarrow \beta_m = 3.74$  for Consequence Class 1, and  $p_m = 10^{-5} \rightarrow \beta_m = 4.26$  for Consequence Class 2) suggested by DNV<sup>[11]</sup> are also incorporated in Fig. 4 for comparison. The results indicate that the current partial safety factor approach used for offshore plate anchor design is conservative over a wide range of  $R_{D/T}$  values, particularly for lower  $R_{D/T}$ . It should be noted that the same prediction model has been applied to estimate the anchor uplift capacity in the design process and the estimate of failure probabilities, which means that no attempt has been made to consider uncertainties associated with the geotechnical prediction model in this analysis. As discussed previously, the upper bounds of the coefficients of variation of  $F_T$  and  $F_D$  have been conservatively applied in this analysis. These conservative and unconservative factors generally cancel one another out to some extent.



**Fig. 4 Reliability index of designed strip plate anchors for uplift limit state**

### 7 Conclusions

This study conducted a reliability analysis of designing strip plate anchors in sand for uplift limit state under pure vertical loading. To achieve this, the partial safety factor approach was first applied to calculate the required anchor embedment depth, which was then employed to estimate the failure probability of the designed anchor using Monte Carlo simulations. This analysis considered two consequence classes corresponding to two different sets of partial safety factors and target acceptable failure probabilities. A wide range of  $R_{D/T}$  values was taken to investigate its effect on the estimation of failure probability.

The results suggest that the estimated reliability index decreases rapidly with increasing the ratio  $R_{D/T}$  for  $R_{D/T} < 1.5$  and gradually converges to a relatively steady state, because the more variable  $F_D$  becomes more dominant

than  $F_T$  with the increase of  $R_{D/T}$ . Compared to the target failure probabilities suggested by DNV<sup>[11]</sup>, the current partial safety factor approach used for offshore plate anchor design is conservative over a wide range of  $R_{D/T}$  values, particularly for lower  $R_{D/T}$ . It is worth noting that the reliability index may be conservatively estimated for several reasons. One is that, the upper bounds of the coefficients of variation of  $F_T$  and  $F_D$  have been applied. In addition, the positive correlation between  $\varphi_p$  and  $\gamma'$  has been ignored, which is likely to overestimate the calculated failure probabilities<sup>[23]</sup>. On the other hand, the uncertainties related to the uplift capacity prediction model have not been accounted for. Thus, further work is required to examine whether the partial safety factor method is still overly conservative when considering all these conservative and unconservative factors. In addition, for practical applications, a more accurate estimate of  $R_{D/T}$  is essential to determine the required partial safety factors.

In general, these conservative and unconservative factors cancel one another out to some extent, and the current results are considered to be reasonably accurate and can provide probabilistic insights and guidance into the reliability of plate anchors for offshore wind turbines.

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